

## The Crystal and Molecular Structures of *N*-Acetyl-DL-alanine-*N*-methylamide and *N*-Acetyl-L-alanine-*N*-methylamide

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Crystals of the DL compound (DL-AANMA) grown from an acetone solution belong to the tetragonal space group  $I4_1/a$  with  $a = 13.81$  (3),  $c = 16.50$  (3) Å (at room temperature),  $Z = 16$  and those of the L compound (L-AANMA) grown from a methanol solution belong to the orthorhombic space group  $P2_12_12_1$  with  $a = 13.87$  (7),  $b = 6.98$  (4),  $c = 16.29$  (8) Å,  $Z = 8$ . The structure of DL-AANMA was solved by the method of symbolic addition and refined by the full-matrix least-squares procedure based on the diffractometer data obtained at  $-137^\circ\text{C}$ . The final  $R$  value was 0.072 allowing for the anisotropic thermal vibrations for each atom and for the disorder of the structure. The structure of L-AANMA was derived from that of DL-AANMA and refined by the full-matrix least-squares method based on the photographic data. The final  $R$  value was 0.12 assuming isotropic thermal vibrations for each atom. The  $\varphi_{\text{CN}}$  and  $\psi_{\text{CC}}$  values of the L molecules found in both crystals deviate, from those of the ideal straight-chain conformation, to the right in the Ramachandran plot, resulting in a right-hand twist of the peptide chain. In both crystals, the molecules are hydrogen-bonded, as in the  $\beta$ -pleated sheet structure, but the sheet is twisted to form a left-hand helical unit (for L-molecules) along the  $c$  axis. The helical unit in L-AANMA is derived from the antiparallel-chain pleated sheet while that in DL-AANMA from the parallel-chain pleated sheet. In the latter unit, about 10% of the antiparallel chains are mixed, giving rise to disorder in the structure.

### Introduction

In the course of a study on infrared spectra of crystalline *N*-acetyl-alanine-*N*-methylamide,  $\text{CH}_3\text{CONHCH}_2\text{CH}_2\text{CONHCH}_3$ , Koyama, Shimanouchi, Sato & Tatsuno (1971) found two crystalline modifications, forms I and II. These two forms differ in their skeletal vibrations, as shown by the differences in the frequencies of the amide IVa and VIa bands. This paper describes the result of the crystal structure determinations of form I of both *N*-acetyl-DL-alanine-*N*-methylamide (DL-AANMA) and *N*-acetyl-L-alanine-*N*-methylamide (L-AANMA).

### Experimental

The crystals of DL-AANMA and L-AANMA were grown from acetone and methanol solutions respectively. For both compounds they are transparent colourless prisms elongated along the  $c$  axis. The density was measured by the flotation method in a mixed solution of dichloroethane and benzene. Lattice constants and intensity data of DL-AANMA were obtained on a Rigaku four-circle X-ray diffractometer at room temperature and later at  $-137^\circ\text{C}$ . In the latter case, the specimen was cooled by blowing evaporated liquid nitrogen from a Dewar vessel and the temperature was measured by a copper-constantan thermocouple placed very near the specimen. Intensities were measured by the  $\omega$ - $2\theta$  scanning method with a scan speed of  $4^\circ 2\theta \text{ min}^{-1}$ . The background was measured at both sides of each diffraction peak for 10 s.

In the case of L-AANMA, although the crystals were well developed prisms in appearance,  $c$  axis Weissenberg photographs showed an elongation of the spots in a horizontal direction indicating that the crystal is composed of fragments aligned along  $c$  but disoriented in the perpendicular direction. The angular divergence was estimated from the lengths of the spots to be about  $10^\circ$  around the  $c$  axis. Trials to find better crystals were not successful and the intensities were recorded by the multiple-film method on equi-inclination Weissenberg photographs for the layers 0 and 1 around the  $a$  axis and 0 to 6 around the  $c$  axis. Because of the disorientation and the large temperature factor of the crystal, the intensities faded out rapidly in the high-angle region.

Crystal data and the intensity-data measurements are summarized in Table 1.

### Determination of the structures

#### DL-AANMA

The structure was solved by the symbolic addition method (Karle & Karle, 1966) with the room-temperature data. The refinement was carried out by the block-diagonal least-squares method. During the refinement a difference Fourier map was calculated which revealed, besides a few unexplained peaks, eight hydrogen atoms out of twelve contained in an asymmetric unit. The  $R$  value was reduced to 0.08 when anisotropic temperature factors were assigned to the heavy atoms and isotropic ones to the hydrogen atoms. The bond lengths and angles, however, revealed some unexpected

values, mostly for the amide groups. A difference Fourier map calculated with the final set of parameters still showed a few unexplained peaks of about  $1 e \text{ \AA}^{-3}$  near the amide groups, but it was not possible to interpret the peaks as hydrogen atoms. The situation was not improved when the refinement was carried out with the low-temperature data.

On completion of the structure determination of L-AANMA, we discovered that the structural unit in L-AANMA is very similar to that in DL-AANMA. They differ in that while the L-structural unit in DL-AANMA has  $4_3$  symmetry, the unit in L-AANMA has  $2_1$  symmetry and the two crystallographically independent molecules,  $M_1$  and  $M_2$ , are arranged alternately. Of particular interest was the orientation of  $M_2$ , which is the reverse of that expected for the molecule related to  $M_1$  by  $4_3$  symmetry. This attracted our attention and we tried to refine the structure of DL-AANMA assuming that a molecule, designated  $M_{rev}$ , was in the reverse orientation, as shown in Fig. 1.

Refinement was further continued for the disordered structure in which a fraction of the molecule  $M_{rev}$  was superposed on the molecule  $M$ . The atomic parameters of  $M_{rev}$  were obtained by rotating  $M$  through an angle

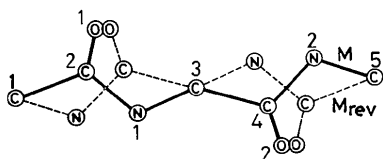


Fig. 1. Superposition of  $M_{rev}$  on the molecule of  $M$  assumed for the disordered structure of DL-AANMA.

of  $180^\circ$  about C(3) ( $\alpha$ -carbon) while the positions of the terminal carbon atoms remain unchanged; a small adjustment of the coordinates was necessary to explain the spurious peaks in the difference Fourier map. Several sets of full-matrix least-squares refinement were then calculated based on the low-temperature intensity data. In each set the atomic parameters and the occupancy factor of  $M_{rev}$  were fixed, but the latter was increased stepwise by 0.01 from set to set. The minimum value of  $R$ , 0.072, was obtained when the occupancy factor reached 0.1. The weight function used for the calculation was:

$$v_w = F_o/20, \text{ when } F_o < 20, \\ v_w = 1, \text{ when } 20 \leq F_o \leq 300, \\ v_w = 1/\{1 + 0.02(F_o - 300)\}, \text{ when } F_o > 300.$$

The final atomic parameters for  $M$  and  $M_{rev}$  are given in Table 2. A comparison of the observed (at  $-137^\circ\text{C}$ ) and calculated structure factors is shown in Table 3.

#### L-AANMA

An interesting correlation involving the lattice constants and space-group symmetries (shown in Fig. 2) for the crystals of DL-AANMA and L-AANMA led us to suppose that a structural unit found in DL-AANMA about the  $4_3$  axis would also exist in L-AANMA about the  $2_1$  axis. Indeed, the infrared spectra observed for both crystals were so alike that a similar conformation and a similar environment of the molecules were suggested for L-AANMA. An  $R$  map was therefore calculated for the 151 strongest three-dimensional reflexions in the low  $2\theta$ -angle region. The starting model was constructed by assuming the same molecular structure

Table 1. Crystal data and measurement of intensity data

<i>N</i> -Acetyl-DL-alanine- <i>N</i> -methylamide (DL-AANMA)		$\text{C}_6\text{H}_{12}\text{N}_2\text{O}_2$ , M.W. 144.2	L-AANMA
<i>N</i> -Acetyl-L-alanine- <i>N</i> -methylamide (L-AANMA)			
	DL-AANMA		
	At room temperature	At $-137^\circ\text{C}^*$	
Crystal system	Tetragonal		Orthorhombic
Space group	$I4_1/a$		$P2_12_12_1$
$a$ ( $\text{\AA}$ )	13.81 (3)	13.615 (10)	13.87 (7)
$b$ ( $\text{\AA}$ )	13.81 (3)	13.615 (10)	6.98 (4)
$c$ ( $\text{\AA}$ )	16.50 (3)	16.435 (10)	16.29 (8)
$U$ ( $\text{\AA}^3$ )	3144	3046.5	1579
$U/\text{molec.}$ ( $\text{\AA}^3$ )	196.5	190.41	197.4
$D_m$ ( $\text{g cm}^{-3}$ )	1.216		1.216
$D_x$ ( $\text{g cm}^{-3}$ )	1.219		1.214
$Z$		16	8
Intensity measurement	Diffractometer		Weissenberg camera
Radiation	Ni-filtered Cu $K\alpha$		Ni-filtered Cu $K\alpha$
Number of reflexions observed	812	811	372
% of the total	60	60	34
$2\theta$ less than	$130^\circ$	$130^\circ$	$80^\circ$
Overall $B$ ( $\text{\AA}^2$ ) (from Wilson plot)	4.5	2.6	6.9

\* The specimen was not identical with that used for the room-temperature measurement though the conditions of crystallization were the same.

Table 2. Final atomic parameters for DL-AANMA at -137°C

Temperature factors are of the form  $T = \exp [-(\beta_{11}h^2 + \beta_{22}k^2 + \beta_{33}l^2 + 2\beta_{12}hk + 2\beta_{13}hl + 2\beta_{23}kl)]$ . All parameters are multiplied by  $10^4$  except for  $B$ , and the e.s.d.'s are given in parentheses denoting the least significant digits.

	<i>x</i>	<i>y</i>	<i>z</i>	$\beta_{11}$	$\beta_{22}$	$\beta_{33}$	$\beta_{12}$	$\beta_{13}$	$\beta_{23}$
<i>M</i> (occupancy factor=0.9)									
C(1)	1535 (4)	1659 (5)	1764 (3)	32 (4)	49 (4)	18 (3)	0 (3)	-4 (2)	1 (2)
C(2)	1704 (5)	947 (6)	2496 (4)	25 (4)	49 (5)	24 (3)	-9 (4)	4 (3)	-10 (3)
C(3)	1642 (5)	-704 (4)	2954 (4)	47 (4)	21 (4)	26 (3)	5 (3)	-7 (3)	-3 (2)
C(4)	2666 (6)	-986 (5)	3182 (4)	68 (6)	11 (4)	27 (3)	-8 (4)	-20 (3)	1 (3)
C(5)	3811 (5)	-1656 (5)	4161 (4)	51 (5)	44 (4)	32 (3)	11 (4)	-15 (3)	4 (3)
C(6)	1036 (7)	-1611 (7)	2744 (5)	76 (7)	65 (6)	39 (4)	-20 (5)	-16 (4)	10 (4)
N(1)	1558 (4)	31 (4)	2362 (3)	45 (4)	34 (4)	21 (3)	3 (3)	6 (2)	1 (2)
N(2)	2870 (5)	-1305 (4)	3914 (3)	54 (4)	48 (4)	24 (3)	1 (3)	-2 (3)	-3 (2)
O(1)	1923 (4)	1274 (3)	3166 (2)	54 (3)	44 (3)	11 (2)	-7 (3)	-9 (2)	-3 (2)
O(2)	3355 (4)	-1002 (4)	2625 (3)	75 (4)	64 (4)	20 (3)	-3 (3)	13 (2)	9 (2)

Table 2 (cont.)

*M*<sub>rev</sub> (occupancy factor=0.1)

All parameters are assumed values except for the occupancy factor.

C(11)	3811	-1656	4161	$B = 3.5 \text{ \AA}^2$
C(12)	3234	-1241	3425	3.5
C(13)	1642	-704	2954	3.5
C(14)	1718	382	2774	3.5
C(15)	1535	1659	1764	3.5
C(16)	584	-976	3114	3.5
N(11)	2265	-1067	3619	3.5
N(12)	1520	620	2000	3.5
O(11)	3558	-1074	2719	3.5
O(12)	1944	999	3310	3.5

Table 3. Observed and calculated structure factors of DL-AANMA

Table with multiple columns of numerical data representing observed and calculated structure factors for DL-AANMA. The data is organized in a grid-like format with several columns of values.

and the same relationship to the screw axis as found for *M* in the crystal of DL-AANMA. The molecule was then rotated around the 2<sub>1</sub> axis through an angle of  $\pi/2$  at intervals of 0.05 rad. In each case, the molecule was translated along the *c* axis from *z*=0 to 0.5 at intervals of 0.02 (0.32 Å). In this calculation, although there is no need to assume the equivalence of the two successive molecules along the 2<sub>1</sub> axis, it was assumed

that they were still in positions related by a 4<sub>3</sub> symmetry.

A plausible structure obtained from the *R* map gave a minimum *R* value of 0.36. This structure was then refined in the usual way by the least-squares method. In the course of the refinement, it became clear that the model could not be refined beyond the *R* value of 0.23 and that it also gave unreasonable bond lengths and angles. A difference Fourier map showed some unusual features which were interpretable as being one of the two crystallographically independent molecules about the 2<sub>1</sub> axis replaced by the molecule having the reversed orientation. This structure could be refined by the full-matrix least-squares method to an *R* value of 0.12 excluding hydrogen atoms. In this calculation, only individual isotropic thermal parameters were assumed because of the limited number of reflexions in the high-angle region. The weighting function was:

$$w = \begin{cases} F_o/10, & \text{when } F_o < 10, \\ 1, & \text{when } 10 \leq F_o \leq 30, \\ 1/\{1 + 0.02(F_o - 30)\}, & \text{when } F_o > 30. \end{cases}$$

The final atomic parameters are listed in Table 4 and the observed and calculated structure factors in Table 5.

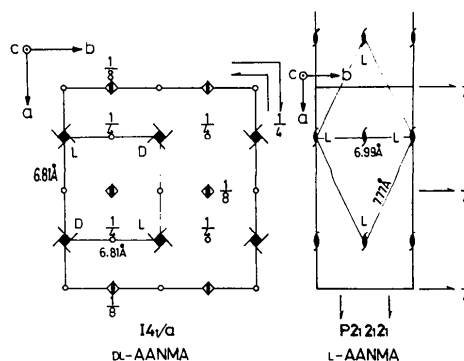


Fig. 2. Comparison of the space-group symmetries between the crystals of DL- and L-AANMA. D and L denote the helical units consisting of D and L molecules respectively. In each unit, the helix axis is coincident with the crystallographic tetrad or diad screw axis.

Table 4. Final atomic parameters for L-AANMA

	x	y	z	B
$M_1$				
C(1)	563 (24)	1200 (52)	8176 (24)	4.6 (1.0)
C(2)	1313 (34)	1154 (64)	7505 (34)	7.2 (1.2)
C(3)	2944 (27)	2011 (54)	7040 (24)	4.8 (1.0)
C(4)	3372 (29)	-87 (70)	6822 (30)	7.6 (1.3)
C(5)	4320 (29)	-2146 (61)	5882 (25)	6.5 (1.2)
C(6)	3689 (27)	3174 (51)	7373 (27)	5.9 (1.1)
N(1)	2198 (23)	1656 (40)	7702 (20)	4.8 (0.8)
N(2)	3807 (21)	-297 (45)	6092 (22)	5.2 (0.9)
O(1)	1047 (18)	901 (37)	6750 (21)	6.5 (0.8)
O(2)	3424 (19)	-1370 (44)	7368 (19)	7.6 (0.9)
$M_2$				
C(11)	3526 (22)	3635 (46)	3516 (21)	3.4 (0.9)
C(12)	3057 (38)	2729 (69)	4261 (37)	10.1 (1.5)
C(13)	1555 (26)	981 (52)	4745 (25)	5.8 (1.1)
C(14)	1851 (38)	-1117 (76)	4826 (38)	9.8 (1.5)
C(15)	1760 (29)	-3888 (62)	5758 (28)	8.3 (1.3)
C(16)	584 (31)	1475 (59)	4455 (25)	8.3 (1.3)
N(11)	2163 (25)	1919 (42)	4077 (24)	6.6 (0.9)
N(12)	1655 (28)	-1716 (57)	5551 (27)	11.1 (1.3)
O(11)	3312 (17)	2592 (40)	5042 (20)	7.4 (0.7)
O(12)	2313 (17)	-2175 (36)	4307 (17)	7.3 (0.9)

## Discussion of the structure

## Molecular structure

Bond lengths and angles of the AANMA molecules found in the DL and L crystals are compared in Table 6. In general the values agree, but because of the disorder in the crystal of DL-AANMA and because of the large temperature factors in addition to the poor quality of the observed  $F$ 's in L-AANMA, the accuracy in the present structure determination is not high enough to make detailed comparison of the AANMA molecules possible.

The conformations of the four kinds of molecules,  $M$  and  $M_{rev}$  in DL-AANMA (we shall consider only the L molecules in the following discussion), and  $M_1$  and  $M_2$  in L-AANMA are essentially the same and show the distorted  $\beta$  pleated-sheet conformation in proteins. Various torsion angles are listed in Table 7 and the  $\phi, \psi$  values are plotted on the  $\phi$ - $\psi$  chart (Ramachandran, Ramakrishnan & Sasisekharan, 1963) shown in Fig. 3. It is seen that they fall within the upper right part of the allowed region for the  $\beta$  structure. The planarities of the peptide groups are shown in Table 8 and the dihedral angles at the  $C^\alpha$  atom between the two peptide planes are listed in Table 7 together with other parameters characterizing the structure of peptides. The dihedral angles in the AANMA molecules are much larger than those found in other polypeptide molecules, suggesting that the AANMA molecules are more strongly folded, although the distances between the terminal carbon atoms which correspond to the repeat distance of the peptide backbone do not differ very much from the normal value. This is en-

Table 5. Observed and calculated structure factors of L-AANMA

h	k	l	$F_o$	$F_c$	$R$
1	0	0	100	100	0.00
2	0	0	100	100	0.00
3	0	0	100	100	0.00
4	0	0	100	100	0.00
5	0	0	100	100	0.00
6	0	0	100	100	0.00
7	0	0	100	100	0.00
8	0	0	100	100	0.00
9	0	0	100	100	0.00
10	0	0	100	100	0.00
11	0	0	100	100	0.00
12	0	0	100	100	0.00
13	0	0	100	100	0.00
14	0	0	100	100	0.00
15	0	0	100	100	0.00
16	0	0	100	100	0.00
17	0	0	100	100	0.00
18	0	0	100	100	0.00
19	0	0	100	100	0.00
20	0	0	100	100	0.00
21	0	0	100	100	0.00
22	0	0	100	100	0.00
23	0	0	100	100	0.00
24	0	0	100	100	0.00
25	0	0	100	100	0.00
26	0	0	100	100	0.00
27	0	0	100	100	0.00
28	0	0	100	100	0.00
29	0	0	100	100	0.00
30	0	0	100	100	0.00
31	0	0	100	100	0.00
32	0	0	100	100	0.00
33	0	0	100	100	0.00
34	0	0	100	100	0.00
35	0	0	100	100	0.00
36	0	0	100	100	0.00
37	0	0	100	100	0.00
38	0	0	100	100	0.00
39	0	0	100	100	0.00
40	0	0	100	100	0.00
41	0	0	100	100	0.00
42	0	0	100	100	0.00
43	0	0	100	100	0.00
44	0	0	100	100	0.00
45	0	0	100	100	0.00
46	0	0	100	100	0.00
47	0	0	100	100	0.00
48	0	0	100	100	0.00
49	0	0	100	100	0.00
50	0	0	100	100	0.00
51	0	0	100	100	0.00
52	0	0	100	100	0.00
53	0	0	100	100	0.00
54	0	0	100	100	0.00
55	0	0	100	100	0.00
56	0	0	100	100	0.00
57	0	0	100	100	0.00
58	0	0	100	100	0.00
59	0	0	100	100	0.00
60	0	0	100	100	0.00
61	0	0	100	100	0.00
62	0	0	100	100	0.00
63	0	0	100	100	0.00
64	0	0	100	100	0.00
65	0	0	100	100	0.00
66	0	0	100	100	0.00
67	0	0	100	100	0.00
68	0	0	100	100	0.00
69	0	0	100	100	0.00
70	0	0	100	100	0.00
71	0	0	100	100	0.00
72	0	0	100	100	0.00
73	0	0	100	100	0.00
74	0	0	100	100	0.00
75	0	0	100	100	0.00
76	0	0	100	100	0.00
77	0	0	100	100	0.00
78	0	0	100	100	0.00
79	0	0	100	100	0.00
80	0	0	100	100	0.00
81	0	0	100	100	0.00
82	0	0	100	100	0.00
83	0	0	100	100	0.00
84	0	0	100	100	0.00
85	0	0	100	100	0.00
86	0	0	100	100	0.00
87	0	0	100	100	0.00
88	0	0	100	100	0.00
89	0	0	100	100	0.00
90	0	0	100	100	0.00
91	0	0	100	100	0.00
92	0	0	100	100	0.00
93	0	0	100	100	0.00
94	0	0	100	100	0.00
95	0	0	100	100	0.00
96	0	0	100	100	0.00
97	0	0	100	100	0.00
98	0	0	100	100	0.00
99	0	0	100	100	0.00
100	0	0	100	100	0.00

Table 6. Bond lengths and angles

Bond lengths (Å)	DL-AANMA (at $-137^\circ\text{C}$ )		L-AANMA		Peptide model*
	$M$	$M_{rev}$ (assumed)	$M_1$	$M_2$	
C(1)-C(2)	1.562 (9)	1.549	1.51 (6)	1.51 (3)	1.53
C(2)-N(1)	1.282 (9)	1.378	1.32 (6)	1.40 (4)	1.32
C(2)-O(1)	1.225 (8)	1.262	1.30 (6)	1.32 (3)	1.24
C(3)-C(4)	1.494 (10)	1.512	1.62 (6)	1.53 (4)	1.53
C(3)-C(6)	1.525 (11)	1.510	1.43 (5)	1.47 (6)	
C(3)-N(1)	1.400 (8)	1.469	1.52 (5)	1.53 (4)	1.47
C(4)-N(2)	1.310 (9)	1.340	1.34 (6)	1.28 (4)	1.32
C(4)-O(2)	1.311 (9)	1.256	1.26 (6)	1.29 (3)	1.24
C(5)-N(2)	1.426 (9)	1.467	1.51 (5)	1.56 (6)	1.47
Bond angles ( $^\circ$ )					
N(1)-C(2)-C(1)	116.6 (0.6)	111.6	117 (4)	112 (1)	114
N(1)-C(2)-O(1)	123.1 (0.7)	121.1	122 (4)	115 (1)	125
C(1)-C(2)-O(1)	120.2 (0.6)	127.3	120 (4)	133 (2)	121
C(4)-C(3)-C(6)	110.7 (0.6)	109.8	110 (3)	120 (3)	
N(1)-C(3)-C(6)	112.2 (0.6)	109.8	109 (3)	100 (3)	
N(1)-C(3)-C(4)	115.7 (0.5)	115.8	105 (3)	109 (2)	111
N(2)-C(4)-C(3)	120.9 (0.6)	114.1	117 (4)	110 (2)	114
N(2)-C(4)-O(2)	119.0 (0.6)	123.6	121 (4)	121 (2)	125
C(3)-C(4)-O(2)	119.8 (0.6)	122.3	121 (4)	129 (2)	121
C(2)-N(1)-C(3)	124.3 (0.6)	116.0	121 (3)	121 (1)	123
C(4)-N(2)-C(5)	124.3 (0.6)	118.8	120 (3)	120 (3)	123

\* Pauling &amp; Corey (1953).

tirely due to deformation of the backbone conformation which can be seen in their  $\varphi$  and  $\psi$  values. A similar deformation characterized by the deviation of  $\varphi, \psi$  values from those of the ideal straight chain (number of residues per turn,  $n=2$ ) to the right in the Ramachandran plot is often observed in the  $\beta$  pleated sheets in globular proteins, as indicated recently by Chothia (1973), who has also shown that the deformation causes the polypeptide chain to twist in a clockwise direction when viewed along the chain and that the chains with such a right-hand twist are energetically more favoured than those without twist or with a left-hand twist. It is interesting to see that even such a small polypeptide as AANMA, having only one amino acid residue with two peptide groups, exhibits a tendency to take a right-hand twist. Furthermore, the deviations of the  $\varphi, \psi$  values from the line  $n=2$  and hence the twist of the chain are much more exaggerated in AANMA than in the globular proteins mentioned by Chothia. As a result of the large deviations, the conformation of the molecules of AANMA resembles more that of polyglycine II or collagen, as shown in Fig. 4.

#### Crystal structure

Figs. 5 and 6 are perspective drawings of the structural units in DL- and L-AANMA drawn by the ORTEP program (Johnson, 1965). In these units, the molecules are arranged in such a way that the hydrogen-bonded sheets similar to the  $\beta$  pleated sheets are twisted to form a helical unit along the  $c$  axis, the long axis of the molecules being nearly perpendicular to the helix axis. In DL-AANMA, the D and L molecules form different units mutually antipodal and arranged as shown in Fig. 2.

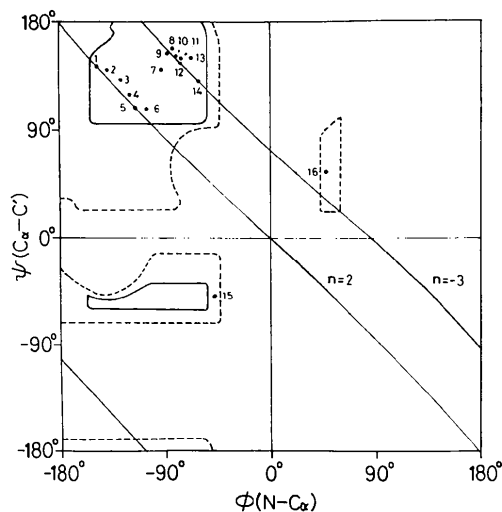


Fig. 3. The Ramachandran plot showing the backbone conformation of various peptides. The solid line encloses the fully allowed regions and broken line outer-limit regions. Contours of constant  $n$  (number of residues per turn) represent the conformations having the same  $n$  values. The right-hand helices take the positive  $n$ . (1) Antiparallel chain pleated sheet (Pauling & Corey, 1953); (2) Poly-L-alanine (Marsh, Corey & Pauling, 1955); (3) Glycylphenylalanylglycine (Marsh & Glusker, 1961); (4) *N*-Acetyl-DL- $\alpha$ -amino *n*-butyric acid-*N*-methylamide (Koyama, Shimanochi, Sato & Tatsuno, 1971); (5) Parallel chain pleated sheet (Pauling & Corey, 1953); (6) *N*-Acetyl-DL-phenylalanine-*N*-methylamide (Harada & Iitaka, 1974); (7) *N*-Acetyl-DL-leucine-*N*-methylamide (Ichikawa & Iitaka, 1969); (8) *N*-Acetyl-L-alanine-*N*-methylamide ( $M_1$ ) (present study); (9) *N*-Acetyl-L-alanine-*N*-methylamide ( $M_2$ ) (present study); (10) *N*-Acetyl-DL-alanine-*N*-methylamide ( $M_{rev}$ ) (present study); (11) *N*-Acetyl-DL-alanine-*N*-methylamide ( $M$ ) (present study); (12) Polyglycine II (Crick & Rich, 1955); (13) *N*-Acetyl-glycine-*N*-methylamide (Iwasaki, 1972); (14) Collagen helix (Sasisekharan, 1962); (15) Right-handed  $\alpha$ -helix (Pauling & Corey, 1951); (16) Left-handed  $\alpha$ -helix.

Table 7. Torsion angles and distortions in hydrogen bonds

	DL-AANMA*		L-AANMA		Poly-L-alanine	ACP	PCP	Polyglycine II	Collagen
	$M$	$M_{rev}$	$M_1$	$M_2$					
$\varphi$	-75.9°	-80.5°	-84.3°	-87.6°	-139.5°	-145°	-119°	-77°	-62°
$\psi$	150.1	152.0	159.0	154.8	140.5	142	113	145	131
$\omega_1$	-177.7	-177.9	-168.4	-178.2	-176.3	180	180	179	
$\omega_2$	175.3	177.9	173.3	171.9	-176.3	180	180	179	
$\theta$	86.3	86.8	94.2	85.3	43.3	43.5	63.5	90.1	
C(1)-C(5)	6.75 Å	6.75 Å	6.82 Å	6.85 Å	6.95 Å	7.00 Å	6.5 Å	6.5 Å	
O...N	2.94	2.9†	2.80	2.92	2.77	2.76	2.82	2.77	
	2.80	2.7†	2.73	2.72	2.77				
$\angle(O=C...N)$	21.4°	16°	33.6°	29.5°	1.2°	1°	17°	5°	
	34.6	31	29.8	32.7	1.2				
$\angle(C=O...N)$	149.7	156	131.6	138.3	178.2	178	156	173	
	130.0	134	136.2	132.4	178.2				
References	(1)		(2)		(3)	(4)	(5)	(6)	(7)

\* For L molecules

† Between  $M_{rev}$  molecules

$$\varphi = \tau[C(2)-N(1)-C(3)-C(4)] \quad \psi = \tau[N(1)-C(3)-C(4)-N(2)]$$

$$\omega_1 = \tau[C(1)-C(2)-N(1)-C(3)] \quad \omega_2 = \tau[C(3)-C(4)-N(2)-C(5)]$$

$\theta$ : Dihedral angle between the peptide groups I and II

C(1)-C(5): Distance between C(1) and C(5) or the chain repeat distance

References: (1), (2) Present study; (3) Marsh, Corey & Pauling (1955); (4), (5) Pauling & Corey (1953); (6) Crick & Rich (1955); (7) Sasisekharan (1962).

Of particular interest is that (a) while the unit in DL-AANMA is derived by twisting the parallel-chain pleated sheet (PCP), that in L-AANMA is derived by twisting the antiparallel-chain pleated sheet (ACP), and (b) the hydrogen bonds connecting the two successive molecules are equally well formed, as shown in Figs. 5 and 6. The energy difference between the

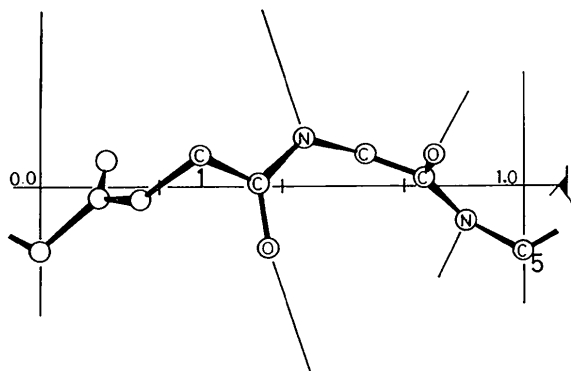


Fig. 4. Structure of polyglycine II showing a similar backbone conformation to that of L-AANMA. Two successive residues ( $C_1 \sim C_5$ ) can be compared with the L-AANMA molecule shown at the top of Fig. 6. The six hydrogen bonds involved in one turn of the polyglycine helix link the six surrounding helices respectively to form a crystalline fibre.

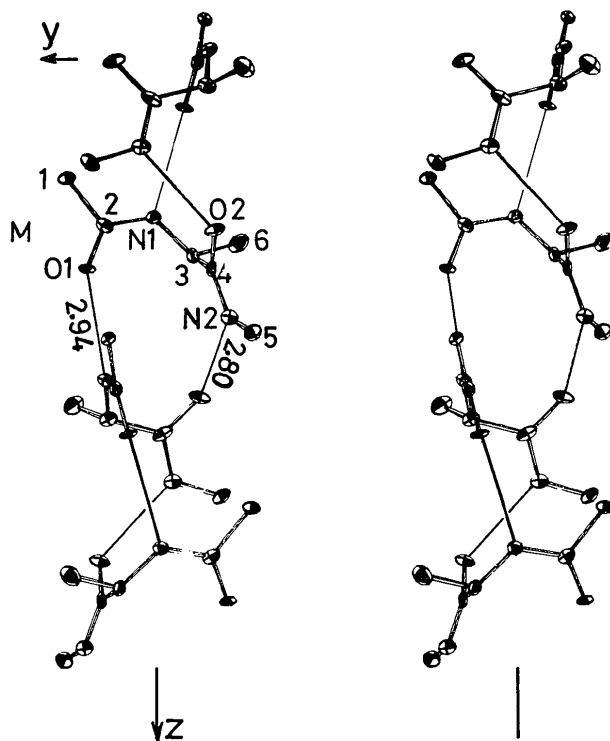


Fig. 5. A stereoscopic drawing of the helical unit of L molecules found in DL-AANMA viewed along the  $a$  axis. The atoms are drawn with 13% probability ellipsoids. Hydrogen bonds are shown as single thin lines.

PCP and ACP structures may not be large, since the structures of DL- and L-AANMA show a close resemblance and since a fraction of the ACP structure is mixed in the crystal of DL-AANMA.

Table 8. Least-squares planes through the peptide groups

DL-AANMA		
Molecule $M$		
Peptide group I: (1) C(1), C(2), C(3), N(1), O(1)	(2) 0.012	(3) $0.965X - 0.103Y - 0.241Z = 1.099$
Peptide group II: (1) C(3), C(4), C(5), N(2), O(2)	(2) 0.024	(3) $0.233X + 0.935Y + 0.266Z = 0.942$
Molecule $M_{rev}$		
Peptide group I: (1) C(11), C(12), C(13), N(11), O(11)	(2) 0.011	(3) $0.227X + 0.935Y + 0.274Z = 0.954$
Peptide group II: (1) C(13), C(14), C(15), N(12), O(12)	(2) 0.013	(3) $0.965X - 0.104Y - 0.241Z = 1.097$
L-AANMA		
Molecule $M_1$		
Peptide group I: (1) C(1), C(2), C(3), N(1), O(1)	(2) 0.06	(3) $0.237X + 0.963Y + 0.128Z = 1.15$
Peptide group II: (1) C(3), C(4), C(5), N(2), O(2)	(2) 0.04	(3) $0.869X - 0.338Y + 0.362Z = 8.13$
Molecule $M_2$		
Peptide group I: (1) C(11), C(12), C(13), N(11), O(11)	(2) 0.01	(3) $0.446X + 0.873Y - 0.199Z = -1.16$
Peptide group II: (1) C(13), C(14), C(15), N(12), O(12)	(2) 0.04	(3) $0.882X - 0.268Y + 0.388Z = 5.12$

(1) Plane-forming atoms.  
 (2) R.m.s. displacement ( $\text{\AA}$ ) of atoms from the plane.  
 (3) Equation of the plane.  $X$ ,  $Y$  and  $Z$  are along  $a$ ,  $b$  and  $c$  and measured in  $\text{\AA}$ .

Table 9. Interatomic distances less than 3.6  $\text{\AA}$  for DL-AANMA

Between $M$ and $M$		Between $M_{rev}$ and $M_{rev}$	
C(1) $\cdots$ O(1 <sup>i</sup> )	3.51 (1) $\text{\AA}$	C(12) $\cdots$ C(15 <sup>v</sup> )	3.5 $\text{\AA}$
C(3) $\cdots$ O(2 <sup>v</sup> )	3.57 (1)	C(12) $\cdots$ N(12 <sup>v</sup> )	3.5
C(4) $\cdots$ O(2 <sup>v</sup> )	3.57 (1)	C(14) $\cdots$ N(12 <sup>v</sup> )	3.5
C(6) $\cdots$ O(2 <sup>ii</sup> )	3.42 (1)	N(11) $\cdots$ N(12 <sup>v</sup> )	3.4
N(2) $\cdots$ C(1 <sup>v</sup> )	3.60 (1)	N(11) $\cdots$ C(16 <sup>vi</sup> )	3.2
N(2) $\cdots$ C(2 <sup>v</sup> )	3.45 (1)	*N(11) $\cdots$ O(11 <sup>v</sup> )	2.9
N(2) $\cdots$ N(1 <sup>v</sup> )	3.46 (1)	O(11) $\cdots$ C(16 <sup>iii</sup> )	3.1
*N(2) $\cdots$ O(2 <sup>v</sup> )	2.80 (1)	O(12) $\cdots$ C(13 <sup>v</sup> )	3.5
O(1) $\cdots$ C(1 <sup>v</sup> )	3.56 (1)	O(12) $\cdots$ C(14 <sup>v</sup> )	3.5
*O(1) $\cdots$ N(1 <sup>v</sup> )	2.94 (1)	O(12) $\cdots$ C(15 <sup>v</sup> )	3.4
		*O(12) $\cdots$ N(12 <sup>v</sup> )	2.7
Between $M$ and $M_{rev}$			
C(4) $\cdots$ N(12 <sup>v</sup> )	3.50 $\text{\AA}$	O(2) $\cdots$ C(16 <sup>iii</sup> )	3.27
C(6) $\cdots$ O(11 <sup>iii</sup> )	3.30	C(12) $\cdots$ O(1 <sup>v</sup> )	3.54
C(6) $\cdots$ O(11 <sup>iv</sup> )	3.52	C(13) $\cdots$ O(2 <sup>v</sup> )	3.57
C(6) $\cdots$ C(16 <sup>vi</sup> )	3.43	C(15) $\cdots$ O(1 <sup>i</sup> )	3.51
*N(1) $\cdots$ O(12 <sup>vi</sup> )	2.70	C(16) $\cdots$ O(2 <sup>v</sup> )	3.54
N(2) $\cdots$ C(15 <sup>v</sup> )	3.60	N(11) $\cdots$ N(1 <sup>v</sup> )	3.43
N(2) $\cdots$ C(16 <sup>vi</sup> )	3.13	*N(11) $\cdots$ O(2 <sup>v</sup> )	2.72
N(2) $\cdots$ N(12 <sup>v</sup> )	3.27	O(12) $\cdots$ C(1 <sup>v</sup> )	3.40
*N(2) $\cdots$ O(11 <sup>v</sup> )	2.92	O(12) $\cdots$ C(2 <sup>v</sup> )	3.46
O(1) $\cdots$ C(15 <sup>v</sup> )	3.56	O(12) $\cdots$ C(3 <sup>v</sup> )	3.54
*O(1) $\cdots$ N(12 <sup>v</sup> )	2.76	O(12) $\cdots$ C(6 <sup>v</sup> )	3.55
O(1) $\cdots$ C(15 <sup>i</sup> )	3.51		

- (i)  $\frac{1}{2} - x \quad \frac{1}{2} - y \quad \frac{1}{2} - z$  (ii)  $\frac{1}{2} - x \quad -\frac{1}{2} - y \quad \frac{1}{2} - z$   
 (iii)  $\frac{1}{2} + x \quad y \quad \frac{1}{2} - z$  (iv)  $-\frac{1}{2} + x \quad y \quad \frac{1}{2} - z$   
 (v)  $\frac{1}{4} + y \quad \frac{1}{4} - x \quad \frac{1}{4} + z$  (vi)  $\frac{1}{4} + y \quad -\frac{1}{4} - x \quad \frac{3}{4} - z$   
 (vii)  $\frac{1}{4} - y \quad -\frac{1}{4} + x \quad -\frac{1}{4} + z$

\* Hydrogen bond.

As already mentioned, the peptide chain of AANMA has a right-hand twist when viewed along the chain. It follows that the  $\beta$  sheet formed by such chains has a left-hand twist when viewed along the axis perpendicular to the peptide chain (Chothia, 1973). Actually, in the crystals of DL- and L-AANMA, the sense of twist of the helical unit composed of L molecules is left handed. The angle of the twist between the neighbouring molecules along the helix axis is exactly  $90^\circ$  in DL-AANMA.

From the above discussion it would not be surprising to find such a strongly twisted sheet structure for the simple peptide molecules, since the AANMA molecule has only two peptide groups available for the formation of hydrogen bonding and even such a large twist as has been observed in the present crystals does not cause too great a distortion of the hydrogen bonds. Table 7 shows the distortions of the hydrogen bonds in AANMA in comparison with those found in related polymers.

The short interatomic distances less than  $3.6 \text{ \AA}$  between the molecules are listed in Tables 9 and 10. Since the atoms in  $M_{rev}$  are in the assumed positions, no great significance can be attached to the distances involving  $M_{rev}$ .

Table 10. Interatomic distances less than  $3.6 \text{ \AA}$  for L-AANMA

C(1)····O(12 <sup>ii</sup> )	3.54 (4) Å
C(2)····O(12 <sup>ii</sup> )	3.57 (5)
C(3)····O(11 <sup>i</sup> )	3.32 (5)
C(4)····N(12 <sup>i</sup> )	3.35 (5)
C(4)····O(11 <sup>i</sup> )	3.45 (4)
C(6)····O(12 <sup>ii</sup> )	3.51 (4)
C(11)····O(1 <sup>iii</sup> )	3.54 (5)
N(1)····N(11 <sup>ii</sup> )	3.47 (4)
*N(1)····O(12 <sup>ii</sup> )	2.72 (5)
N(2)····C(14 <sup>i</sup> )	3.46 (4)
N(2)····N(12 <sup>i</sup> )	3.27 (4)
*N(2)····O(11 <sup>i</sup> )	2.73 (4)
O(1)····C(13 <sup>i</sup> )	3.34 (5)
*O(1)····N(12 <sup>i</sup> )	2.80 (3)
*O(2)····N(11 <sup>ii</sup> )	2.92 (3)
O(11)····C(16 <sup>iii</sup> )	3.32 (3)

$$\begin{array}{l} \text{(i)} \quad x \quad y \quad z \\ \text{(ii)} \quad \frac{1}{2}+x \quad \frac{1}{2}-y \quad 1-z \end{array} \quad \text{(ii)} \quad \frac{1}{2}-x \quad -y \quad \frac{1}{2}+z$$

\* Hydrogen bond.

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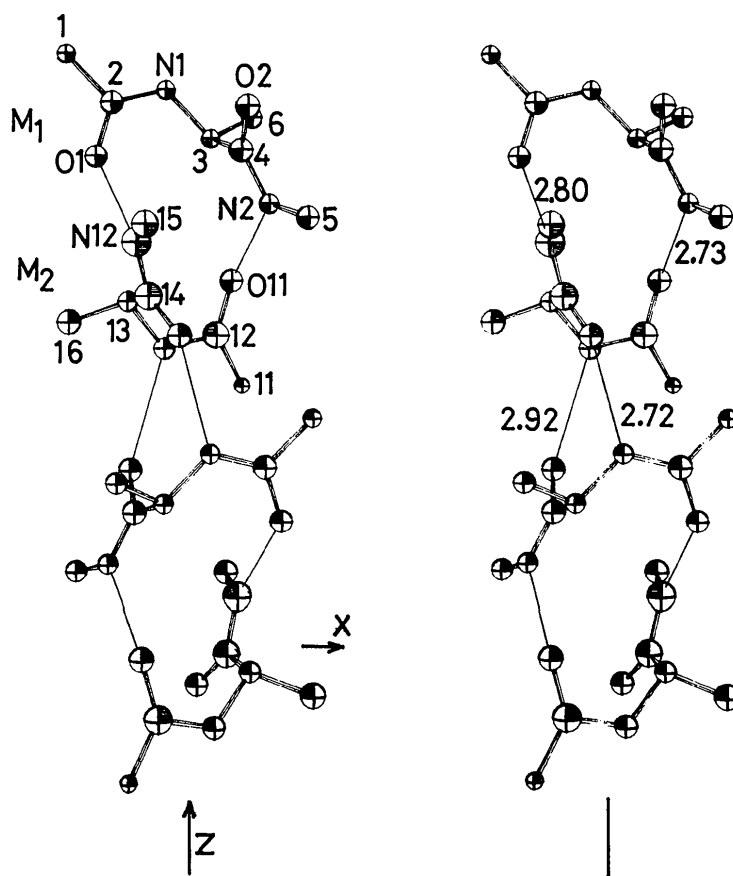


Fig. 6. A stereoscopic drawing of the helical unit found in L-AANMA viewed along the  $b$  axis. The atoms are drawn by 13% probability ellipsoids. Hydrogen bonds are shown as single thin lines.

with the samples and for many valuable discussions. Thanks are also due to Century Research Center for the use of a CDC 6600 computer.

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## Structure Cristalline de la Phase Type 'Bronze de Ruthénium' $\text{Na}_{3-x}\text{Ru}_4\text{O}_9$

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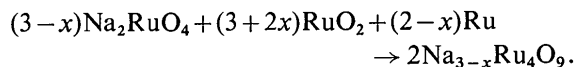
(Reçu le 30 novembre 1973, accepté le 14 février 1974)

The  $\text{Na}_{3-x}\text{Ru}_4\text{O}_9$  ( $x \approx 0.9$ ) phase crystallizes in the monoclinic system. The space group is  $C2/m$ , with  $a = 23.180 \pm 0.006$ ,  $b = 2.832 \pm 0.002$ ,  $c = 10.990 \pm 0.004$  Å,  $\beta = 104.50^\circ$ . The  $[\text{Ru}_4\text{O}_9]_n^{(3-x)n-}$  network is formed by single, double and triple chains of  $[\text{RuO}_6]$  octahedra sharing edges. These chains are linked together parallel to the  $b$  axis by their corners. The sodium ions are inserted in three different sites in the tunnels.

La synthèse et l'étude structurale de phases oxygénées à base de ruthénium ont été entreprises au laboratoire. Dans le système ternaire sodium–ruthénium–oxygène, de nombreux composés inédits ont été mis en évidence et leurs caractères cristallographiques précisés (Darriet & Galy, 1974; Darriet & Vidal, 1974). C'est ainsi que nous avons mis en évidence, dans le système ternaire  $\text{Na}_2\text{O}-\text{RuO}_2-\text{Ru}_2\text{O}_3$ , à côté de la phase  $\text{NaRu}_2\text{O}_4$  isotype du ferrite  $\text{CaFe}_2\text{O}_4$ , une autre phase originale de formule  $\text{Na}_{3-x}\text{Ru}_4\text{O}_9$ .

#### Préparation et données cristallographiques

$\text{Na}_{3-x}\text{Ru}_4\text{O}_9$  était obtenu à partir de mélanges de  $\text{Na}_2\text{RuO}_4$ , de  $\text{RuO}_2$  et de ruthénium métallique:



Les préparations étaient effectuées en tubes scellés d'or, la montée en température se faisant progressivement par paliers successifs à 500 et 600°C. Le produit de réaction était finalement broyé et maintenu 24 h à 950°C. La phase  $\text{Na}_{3-x}\text{Ru}_4\text{O}_9$  comporte un domaine d'existence correspondant à  $0,25 \geq x \geq 0$ . La poudre bien cristallisée est de couleur bleu acier. Le traitement à

1100°C de la poudre obtenue pour  $x=0,25$  suivi d'un refroidissement lent entraîne la formation de belles aiguilles monocristallines douées d'éclat métallique dont l'axe de croissance correspond à l'axe  $Oy$ .

Les diagrammes de Bragg et de Weissenberg ont permis de préciser, pour l'une d'entre elles, les paramètres  $a$ ,  $b$ ,  $c$  et l'angle  $\beta$  de la maille monoclinique (dimensions:  $0,08 \times 0,01 \times 0,02$  mm). Une seule règle d'extinction a été relevée:

$$hkl: h+k=2n+1.$$

Elle correspond aux groupes spatiaux  $C2$ ,  $Cm$  ou  $C2/m$ . L'ensemble de ces constantes cristallographiques est rassemblé au Tableau 1. Le spectre X de la poudre obtenue après broyage des cristaux a été indexé (Tableau 2).

Tableau 1. Constantes cristallographiques de  $\text{Na}_{3-x}\text{Ru}_4\text{O}_9$

$a$	$= 23,180 \pm 0,006$ Å
$b$	$= 2,832 \pm 0,002$
$c$	$= 10,990 \pm 0,004$
$\beta$	$= 104,50 \pm 0,03^\circ$
	$C2/m$
$d_{\text{calc}}$	$= 5,67$
$Z$	$= 4$